# Increasing Power Density of Single-phase Power Converter by Reduced Passive Components Volume for Short-time Operation

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Abstract— This paper proposes a design concept of shorttime rated ripple current for electrolytic capacitors and the concept method of inductors that accepts a magnetic saturation in order to reduce the volume of passive components. The shorttime rated ripple current for DC-link capacitors is determined by the operation time of power converters and the transient temperature rise characteristic of the electrolytic capacitors with the ripple current exceeding the rated current. The relation between the operation time of the power converters and the current value of the electrolytic capacitors is derived by the thermal characteristics of the electrolytic capacitors. The thermal characteristics are obtained by the experiment for the temperature measurement of the element of the electrolytic capacitors. Besides, this paper provides the design concept of the grid-connected inductor from the magnetization characteristic of magnetic materials in order to reduce the size. The effect of the reducing inductor volume by 15% is demonstrated by the calculation with the experimental results.

Keywords— Short-time operation, Passive component, Electrolytic capacitor, magnetic saturation, Interconnected inductor

#### I. INTRODUCTION

Optimization methods of the passive components are crucial for increasing the power density [1-3]. Mainly the power density limit results from the DC-link capacitors in single-phase inverters because the electrolytic capacitors are used as the DC-link capacitors in large-capacity power converters[4]. Some approaches have been proposed in [1-2, 5-7] in order to reduce the DC-link capacitor volume. The volume is reduced by adapting additional circuit in [1-2], and improving control methods in [5]. In [6–7], the optimization methods are proposed by selecting the DC-link capacitors using the capacitors losses or temperature. However, the DClink capacitors is designed to satisfy the rated ripple current of the capacitors in the conventional methods. Thus, the rated ripple current is the constraint to the volume reduction of the DC-link capacitors especially for the electrolytic capacitors. Besides, the grid-connected inductors is also significant problem in terms of the volume reduction of the power converter. Generally, increasing switching frequency or allowing large output current ripples help to reduce the gridconnected inductor volume. The optimization methods of the grid-connected inductors have been proposed from the perspective of EMC[8-11]. However, a minimization of the inductor volume is limited because the grid-connected inductors are generally designed in the linear region of the magnetization characteristics in order to avoid the saturation of the magnetic cores.

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This paper proposes two design methods in order to reduce the passive component volume for the specific power converters, which operate only at the rated power for a shorttime, such as uninterruptible power supplies (UPS) and home appliances compressors. The first method is to adapt the design concept of short-time rated ripple current to the electrolytic capacitors. The electrolytic capacitors allow ripple currents exceeding the rated value based on the transient capacitor temperature. The second method is adapting the design concept of the inductor that allows the magnetic saturation. Allowing magnetic saturation leads to increased losses due to the expanded operating range of the magnetic flux density; however, the increase of losses can be accepted due to the short-time operation. The example of the inductor design using the proposed design method is shown to confirm reducing inductor volume. In addition, the operation of the power converter with the inductors that allow a magnetic saturation is experimentally demonstrated. The originality of this paper is providing a design procedure for the power converters operated for a short-time for downsizing.

# II. REDUCTION METHOD OF DC-LINK CAPACITOR VOLUME

## A. Short-time rated current of electrolytic capacitors

Figure 1 shows the relationship between the ripple current and the temperature rise of the electrolytic capacitors. The temperature rise occurs due to dielectric loss and joule loss on the resistance of terminals or lead wires when a ripple current flows through the electrolytic capacitors. The excessive temperature rise causes failures such as a vent operation due to increasing internal pressure, increasing tan  $\delta$ , and capacitance reduction. The rated ripple current of the electrolytic capacitor is determined by the allowable temperature rise from a maximum category temperature of the electrolytic capacitors. However, the temperature rise does not exceed the allowable temperature rise when the operation time is sufficiently shorter than several times the thermal time constant. Thus, the electrolytic capacitors allow an excess of the ripple current for the short-time operation (the short-time ripple current). The short-time rated ripple current is determined by considering a transient temperature rise characteristic of the electrolytic capacitors. Here, the equivalent series resistance (ESR), thermal resistance, and thermal time constant are assumed as constant values with the temperature change. The heating value of the electrolytic capacitors is the product of the ESR value and the square of XI<sub>rated</sub>, where X is the ratio of the flowing ripple current to the rated ripple current. The temperature rises from the ambient temperature to the steady temperature is the product of the

heating value and the thermal resistance. Thus, the steady temperature  $\Delta T_{steady}$  is given by

$$\Delta T_{steady} = X^2 \Delta T_{rated} = R_{ESR} \left( XI_{rated} \right)^2 R_{th}$$
(1),

where  $\Delta T_{reted}$  is the steady temperature rise when the rated ripple current flows,  $R_{ESR}$  is the ESR value at twice the dominant frequency,  $R_{th}$  is a thermal resistance from an element of the capacitors to an ambient.

From (1), the temperature rise to the steady-state is  $X^2$  times  $\Delta T_{reted}$  when a ripple current that is X times the rated value flows. Therefore, the amount of the transient temperature rise  $\Delta T_{rise}$  is given by

$$\Delta T_{rise} = X^2 \Delta T_{rated} \left\{ 1 - \exp\left(-\frac{\Delta t}{\tau}\right) \right\}$$
(2),

where  $\tau$  is a thermal time constant, and  $\Delta t$  is an operation time of power converters.

From (2), the allowable ripple current ratio X, which is the ratio of the short-time rated ripple current to the rated ripple current, is given by

$$X = \sqrt{\left\{1 - \exp\left(-\frac{\Delta t}{\tau}\right)\right\}^{-1} \frac{\Delta T_{rise}}{\Delta T_{rated}}}$$
(3).

# B. Thermal measurement of electrolytic capacitors

Figure 2 shows the experimental configuration to measure the transient temperature characteristics of the electrolytic capacitors. There are three temperature measurement points for the electrolytic capacitor: the center of the element, the side of the element, and the minus tab. T-type thermocouples are used for temperature measurement. A DC regenerative power supply connected in series with the electrolytic capacitor is used as the power supply as a variable voltage source.

Table 1 shows the experimental conditions. The pulsation voltage of the DC-link capacitor of single-phase power converters is replicated by applying a voltage of 100 Hz AC and DC bias. The ambient temperature is kept constant at 60°C using a constant temperature chamber, assuming that the electrolytic capacitors are used inside a power converter housing. The operable temperature rise is set to  $\Delta T_{rise} = 29^{\circ}$ C based on 60°C due to the maximum allowable electrolytic capacitor temperature.

Figure 3 shows the temperature rise characteristics when the ripple current is twice the rated value. The temperature of the minus tab is the highest in the measurement points. The allowable temperature of the minus tab is sufficiently higher than that of the element using an electrolytic solution. The maximum temperature of the minus tab is required to be around 110°C in order to ignore the effect of the heat dissipation from the minus tab on the life of the electrolytic capacitors. Focusing on the temperature rise of the element of capacitors, the temperature at the center of the element is higher than the temperature at the side of the element. This is because that heat dissipation at the center of the element is harder than at the side of the element in spite of the heat generated by the element of the capacitors is uniform. Thus, it is sufficient to consider the temperature rise characteristic of the center of the element, which is the hottest in the element of the capacitors, when considering the short-time rated



Fig. 1. Relationship between the ripple current and the temperature rise of the electrolytic capacitors.



(a) Temperature measurement point (b) Circuit configuration Fig 2. Experimental configuration to measure capacitor temperature

Table 1. Experimental parameters.			
DC bias voltage	V <sub>dc</sub>	30 V	
Applied voltage	V <sub>sine</sub>	8.1, 16.4, 20.3 V	
Applied frequency	$f_{sine}$	100 Hz	
Applied current	Isine	42.7, 85.4, 106.8 A <sub>ms</sub>	
Capacitor: ECSH401LGN123MFH0N NIPPON CHEMI-CON	С	12 mF	
Capacitor rated voltage	V <sub>rated</sub>	400 V	
Maximum category temperature	Trated	85°C	
Rated ripple current (85°C, $\Delta T$ :10°C)	I rated	42.7 Arms	
Equivalent Series Resistance(ESR) (60 °C, 100 Hz)	R <sub>ESR</sub>	$2.9 \sim 3.3 \text{ m}\Omega$	



Fig. 4. Temperature comparison between calculated value and measured value.

current and the operable time of short-time operation power converters.

Figure 4 shows measurement results and calculation results of temperature rise characteristics with one time, two times, and 2.5 times the rated current. The thermal time constant in calculation results is set to 4150 seconds calculated from the initial temperature to the 63.2% of steady temperature based on the heat generation test result under the condition of 68 A<sub>rms</sub> ( $I_C = 1.6$ p.u.), 40°C and 120 Hz. The thermal resistance from the center of the capacitor to ambient has been obtained from the slope of the approximate curve by plotting the relationship between the heat generation, which is the product of ESR and a ripple current squared, and the steady temperature. The heat capacity has been calculated from the relation between the thermal time constant and thermal resistance.

According to the temperature rise characteristics, the operable time is 2508 seconds in the measurement result and 2587 seconds in the calculation result, which is about 3% longer than the measurement result with 2.5 times the rated current. Therefore, the derived relationship between the short-time rated current and the operable time is confirmed from the experiment. Error factors in calculation results are that the loss caused by the anodic oxide films of the electrolytic capacitors has temperature dependence.

### C. Calculation method of the short-time rated current

The short-time rated current can be obtained by the steady temperature, thermal resistance, and thermal time constant using the heat generation test results for a certain period of time. Thus, doing the heat generation test is not necessary until the time that the temperature rise is saturated. Assuming that ESR, thermal resistance  $R_{th}$ , and thermal time constant  $\tau$  are constant at the time of temperature change, the temperature  $T_{\Delta t}$  after  $\Delta t$  seconds derived by the steady temperature  $T_{steady}$  and the ambient temperature  $T_{ambient}$ , is given by

$$T_{\Delta t} = \left(T_{steady} - T_{ambient}\right) \left\{ 1 - \exp\left(-\frac{t}{\tau}\right) \right\} + T_{ambient}$$
(4).

The following equation is obtained by formula transformation of (4)

$$T_{steady} - T_{\Delta t} = \left(T_{steady} - T_{anbient}\right) \exp\left(-\frac{t}{\tau}\right)$$
(5).

Finding the equation of a natural logarithm on both sides of (5) produces

$$\ln\left(T_{steady} - T_{\Delta t}\right) = \ln\left(T_{steady} - T_{ambient}\right) - \frac{t}{\tau}$$
(6).

The temperature is measured at regular time intervals,  $t = t_1$ ,  $t_2, t_3, ..., t_n$ , in the heat generation test. The following equation is obtained from substituting the two adjacent measurement points  $t_1$  and  $t_2$  into (6) to obtain the difference

$$\ln\left(T_{steady} - T_{\Delta t1}\right) - \ln\left(T_{steady} - T_{\Delta t2}\right) = \frac{1}{\tau} (t_2 - t_1)$$
(7).

Finding the equation of an exponential function on both sides of (7) produces

$$\frac{T_{steady} - T_{\Delta t1}}{T_{steady} - T_{\Delta t2}} = \exp\left(\frac{t_2 - t_1}{\tau}\right)$$
(8).

Furthermore, substituting  $t_2$  and  $t_3$  into (6) to obtain the difference produces

$$\frac{T_{steady} - T_{\Delta L^2}}{T_{steady} - T_{\Delta L^3}} = \exp\left(\frac{t_3 - t_2}{\tau}\right)$$
(9).

Because the right sides of (8) and (9) are equal,  $T_{steady}$  is given by

$$T_{\text{steady}} = \frac{T_{\Delta 1} T_{\Delta 3} - T_{\Delta 2}^{2}}{T_{\Delta 1} + T_{\Delta 3} - 2T_{\Delta 2}}$$
(10).

The steady temperature can be obtained from the heat generation test results in a short time by applying (10) to multiple measurement points and finding the average of the calculated  $T_{steady}$ . The thermal resistance and thermal time constant can be estimated using the obtained steady temperature average  $T_{steady\_avg}$ . The thermal resistance  $R_{th}$  derived ESR and applied current  $I_{ripple}$  is given by

$$R_{th} = \frac{T_{steady}}{R_{ESR} \cdot I_{ripple}^2}$$
(11).

The thermal time constant derived by  $T_{steady\_avg}$ ,  $T_{ambient}$  and the measured temperature  $T_{\Delta tn}$  is given by

$$\frac{t}{\tau} = \ln\left(\frac{T_{\text{steady}\_\text{avg}} - T_{\text{ambient}}}{T_{\text{steady}\_\text{avg}} - T_{\Delta tn}}\right)$$
(12).

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From (12), it can be obtained by substituting the measurement results and calculating the slope by the least-squares approximation since the thermal time constant  $\tau$  is the reciprocal of the slope.

The instance of the calculation the short-time rated current for an operating time of 10 minutes is shown using the measurement results at 2.5 times the rated ripple current. The steady temperature  $T_{steady}$ , thermal resistance  $R_{th}$ , the thermal time constant  $\tau$  are 123.1°C, 1.79 K/W and 3383 seconds using (10), (11) and (12), respectively. The ESR is 3.1 mΩ from table 1. The temperature rise value at the steady temperature with the rated ripple current is  $\Delta T_{rated} = 10.1$ °C substituting the obtained thermal resistance into (1). Assuming that the allowed temperature rise value is 29°C, the short-time rated current is the current at which  $\Delta T_{rise} = 29$ °C at  $\Delta t = 600$  seconds, 10 minutes. The ratio of the short-time rated current to the rated ripple current X derived from (3) is given by

$$X = \sqrt{\left\{1 - \exp\left(-\frac{600}{3884}\right)\right\}^{-1} \frac{29}{10.1}} \approx 4.48$$
 (13).

It can be estimated that the current of 4.48 times the rated ripple current can be accepted as the short-time rated current during a 10-minutes operation.

### D. Expected lifetime during the short-time operation

In order to estimate the expected lifetime of the electrolytic capacitors with a short-time operation, it is necessary to estimate the expected lifetimes when the converter is operating and when it is not operating. In [12], an expected lifetime  $L_X$  (hours) of a screw terminal type electrolytic capacitor derived by an endurance time  $L_e$ , maximum category temperature  $T_{max}$ , ambient temperature  $T_{ambient}$ , temperature rise value with the rated ripple current  $\Delta T_{rated}$ , acceleration factor of an ambient temperature acceleration factor  $K_t$  and derating voltage factor  $K_V$  is given

$$L_{X} = L_{e} \cdot 2^{\frac{K_{e}(T_{max} - T_{andrear})}{10}} \cdot 2^{\frac{\Delta T_{rand} - \Delta T}{A}} \cdot K_{v}$$
(14).

From (14), the expected lifetimes that the converter is operating  $L_{X1}$  and not operating  $L_{X2}$  (shelf lifetime) can be estimated. The combined expected lifetime  $L_{Xcombined}$  of the combined  $L_{X1}$  and  $L_{X2}$  derived the ratio of an operation time  $R_1$ , the ratio of a non-operation time  $R_2$ ,  $L_{X1}$  and  $L_{X2}$  is given by

$$L_{Xcombined} = \frac{1}{\left(\frac{R_{1}}{L_{X1}} + \frac{R_{2}}{L_{X2}}\right)}$$
(15).

Table 2 shows the example of the condition for the estimation to the combined expected lifetime of the electrolytic capacitors using (14). Substituting the conditions into (14), the expected lifetimes during operation  $L_{XI}$  and non-operation  $L_{X2}$  are 26,677 hours and 219,230 hours, respectively. Assuming that the operating time is 10 minutes per day,  $R_1$  and  $R_2$  are 0.69% and 99.31%, respectively. The combined expected lifetime  $L_{Xcombined}$  is about 23.8 years when calculated by substituting into (15).

# III. REDUCTION METHOD OF INTERCONNECTED INDUCTOR VOLUME

# *A.* Design concept of inductors that allow a magnetic saturation

Figure 5 shows the circuit diagram of the grid-tied inverter. The inductance L as the grid-tied inductor is designed under the condition that the allowable ripple current  $r_l$  is satisfied at the point where the maximum value of an inverter output current.

Figure 6 shows the magnetization characteristic of the magnetic material used in a design. In this case, the boundary between the linear region and the non-linear region of the magnetization characteristic is approximately 0.9 T. Non-linearity due to a magnetic saturation is expressed by the function H(B), which is a polynomial approximation of the magnetic field H with the magnetic flux density B. The derivative of H(B) is the reciprocal of the magnetic permeability of an iron core  $\mu_C$ . The effect of air gaps on magnetic permeability is expressed by  $\mu_C$  and the relationship between an iron core magnetic path  $l_C$  and an air gap length  $l_g$ . When  $l_C >> l_g$ , the equivalent magnetic permeability of the core and the air gap, is given by

$$\mu_{eq} = \left(\frac{1}{\mu_{C}} + \frac{l_{g}}{l_{C}\mu_{0}}\right)^{-1} = \left(\frac{dH(B)}{dB} + \frac{l_{g}}{l_{C}\mu_{0}}\right)^{-1}$$
(16),

where  $\mu_0$  is a magnetic permeability in a vacuum.

The integral of the reciprocal of  $\mu_{eq}$  is the equivalent magnetization characteristic  $H_{eq}(B)$ . Thus,  $H_{eq}(B)$  is given by

$$H_{eq}(B) = H(B) + \frac{l_g}{l_C \mu_0} B$$
(17).

Figure 7 shows the shape of the inductor to be designed. It is assumed that the cross-section and the magnetic path of the iron core are square. When  $l_C \gg l_g$ , the volume  $Vol_L$  covered rectangular is approximated by

$$Vol_{L} \approx \left(2\sqrt{A_{W}} + 2\sqrt{A_{C}}\right)\left(\sqrt{A_{W}} + 2\sqrt{A_{C}}\right)\left(2\sqrt{A_{W}} + \sqrt{A_{C}}\right)(18),$$

Table 2. Condition of estimation to the life time with the short-time operation.



where  $A_C$  is a cross-sectional area and  $A_W$  is a window area of the core. The window area  $A_W$  is given by

$$A_W = \frac{I_{out}N}{K_{_W}J} \tag{19},$$

where N is a number of turns of wire, J is a current density of wire,  $K_u$  is a space factor of an inductor,  $I_{out}$  is an RMS output current value.

The cross-sectional area  $A_C$  of the iron core is derived by an allowable magnetic flux density  $B_m$  and an allowable ripple current ratio  $r_l$ . Assuming that there is no leakage in the magnetic field generated by the inductor winding, the crosssection  $A_{Cl}$  derived by  $B_m$  is given by

$$A_{C1} = \left(\frac{\sqrt{2}I_{out}N}{4H(B_m)} - \sqrt{A_w}\right)^2$$
(20).

The ripple magnetic flux density  $\Delta B$  corresponding  $r_I$  is estimated by  $H_{eq}(B)$ . The cross-section  $A_{C2}$  derived by  $\Delta B$  is

given by

$$A_{C2} = \frac{\sqrt{2}V_{Grid} \left(V_{DC} - \sqrt{2}V_{Grid}\right)}{N\Delta B f_{SW} V_{DC}}$$
(21),

where  $V_{DC}$  is an input voltage of a DC-AC converter,  $V_{Grid}$  is a RMS voltage value of a power grid, and  $f_{SW}$  is a switching frequency.

The condition for the inductor to satisfy  $r_I$  is  $A_{C1} \ge A_{C2}$ . Therefore,  $A_C$  is determined by the minimum number of N that satisfies this condition.

Figure 8 shows the example of the ripple current value characteristics according to an inductor current phase  $\theta$  with assuming that a power factor is a unity and an inductance *L* is constant. From (21),  $A_{C2}$  is calculated on the condition that  $\theta = 90$  deg. that a sin wave and a magnetic flux density is maximum. Thus, the considering of the ripple current value characteristics is required when the decreasing of inductance by magnetic saturation is a few henries. Assuming a power factor equals one, a ripple current value  $\Delta I_{ripple}$  derived by  $V_{DC}$  and  $V_{Grid} \sin(\theta)$ , is given by

$$\Delta I_{ripple} = \frac{\sqrt{2}V_{Grid}\sin(\theta) \left(V_{DC} - \sqrt{2}V_{Grid}\sin(\theta)\right)}{Lf_{SW}V_{DC}}$$
(22).

From (22), the phase that a ripple current value is maximum  $\theta_{ripple\_max}$  is given by

$$\theta_{ripple\_max} = \sin^{-1} \frac{V_{DC}}{2\sqrt{2}V_{Grid}}$$
(23).

From (23), the phase that a ripple current value is maximum  $\theta_{ripple\_max}$  equals 90 deg. on the condition that  $V_{DC}$ is higher than  $2\sqrt{2} V_{Grid}$ . Thus, using (21) is only required for the calculation of  $A_{C2}$  on this condition. On the other hand, the calculation of  $A_{C2}$  on this condition. On the other hand, the calculation of  $A_{C2ripple\_max}$  is required for the considering of a ripple current value characteristic on the condition that  $V_{DC}$  is lower than  $2\sqrt{2} V_{Grid}$ . From (21), the cross-section  $A_{C2ripple\_max}$ is calculated by  $\Delta B_{ripple\_max}$  and  $\sqrt{2} V_{Grid} \sin(\theta_{ripple\_max})$ . The ripple magnetic flux density  $\Delta B_{ripple\_max}$  is estimated by  $r_{I}$ ,  $H_{eq}(B)$  and the inductor current that the phase is  $\theta_{ripple\_max}$ . The additional condition for the inductor to satisfy  $r_{I}$  is  $A_{C1} \ge$  $A_{C2ripple\_max}$ .

Figure 9 shows the flowchart of the proposed design method. Considered conditions of the method are an allowable magnetic flux density  $B_m$ , an air-gap length  $l_g$ . Variables are the number of the turn of wire N and the magnetic path length  $l_{Cref}$ . The magnetic mean path length  $l_C$  is calculated from inductors and variables at the estimated volume. The volume is decided when variables satisfy conditions  $A_{C1} \ge A_{C2}$ ,  $A_{C1} \ge A_{C2ripple max}$  and  $l_{Cref} \approx l_C$ .

# B. Design Example

The interconnection inductor is designed using the circuit parameters shown in Figure 5.

Figure 10 shows the calculation results of the inductor volume with changing  $B_m$  from 0.05 to 2.0 T in 0.05 T increments and lg from zero to 30 mm in 0.5 mm increments. The minimum inductor volume is 2.04 L at  $B_m = 1.2$  T and  $l_g = 8.5$  mm. In contrast, the minimum inductor volume is 2.40 L when a non-liner region of magnetization characteristics ( $B_m$ 



is from 0.95 to 2.0 T) is not used. The proposed design method reduces the inductor volume by 15%

# *C. Experiment with inductors that allowed magnetic saturation*

Figure 11 shows the inductance characteristics with the inductor current value  $i_L$  used in the experiment. The required inductance conditions of the used inductor are determined to be two types of inductance to satisfy  $r_I$ . The first is the required inductance without allowing a magnetic saturation  $L_{const}$ . The second is the required inductance with allowing a magnetic saturation on the maximum magnetic flux density  $L_{saturated}$ .  $L_{const}$  is given by

$$L_{const} = \frac{\sqrt{2}V_{Grid}\sin\left(\theta_{ripple\_max}\right)\left(V_{DC} - \sqrt{2}V_{Grid}\sin\left(\theta_{ripple\_max}\right)\right)}{r_{I}I_{Out}f_{SW}V_{DC}}$$
(24).

The inductance  $L_{saturated}$  is derived by the inductance characteristic  $L_{Volmin}(i_L)$  with the calculated inductor shape conditions that the volume is minimum. The inductance characteristic  $L_{Volmin}(i_L)$  derived by the number of turns  $N_{Volmin}$ , the magnetic path length  $l_{C_Volmin}$ , the cross-section  $A_{C_Volmin}$  and the equivalent magnetic permeability with  $\mu_{eq_Volmin}$ , is given by

$$L_{Volmin}\left(i_{L}\right) = \frac{N_{Volmin}^{2} \mu_{eq_{Volmin}}\left(H\left(i_{L}\right)\right) A_{C_{Volmin}}}{l_{C_{Volmin}}}$$
(25).

where  $\mu_{eq\_Volmin}$  is derived by (16) using the magnetic path length  $l_{C\_Volmin}$  and the air-gap length  $l_{g\_Volmin}$ . A magnetic field derived by  $N_{Volmin}$  and  $l_{C\_Volmin}$ , is given by

$$H\left(i_{L}\right) = \frac{N_{Volmin}i_{L}}{l_{C_{Volmin}}}$$
(26).

The inductance  $L_{saturated}$  is the range represented by  $i_L = \sqrt{2} I_{out} \pm 0.5 r_I I_{out}$  in  $L_{Volmin}(i_L)$ .

Figure 12 shows the output current waveform of the experiment with the inductor that allowed magnetic saturation. The ripple current ratio of the inductor current satisfies the condition. In addition, the total harmonic distortion (THD) of the inductor current is 15.1%. Thus, it is confirmed that the desired ripple current ratio can be satisfied by the appropriate inductance characteristics when the reduction of the inductance due to a magnetic saturation is allowed.

### IV. CONCLUSION

This paper proposes the design concept of short-time rated current for the electrolytic capacitors and the estimation method of inductor volume using magnetic saturation. The temperature measurement in the experiment clarifies the derived relationship between the operable time and the short-time current rating. The result is an error of 3% between the measured and calculated operable times under the condition that the current of 2.5 times the rated current is flowing. Besides, the design example of the inductors that allow a magnetic saturation is shown to demonstrate the effect of the proposed design method. The proposed design achieves the reduction of the inductor volume by 15% compared to the volume of non-magnetic saturation design. In addition, the experimental results shows the THD is 15.1% on the same level with the non-saturated inductor.

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Fig. 11. Inductance characteristics of the interconnected inductor. Table 3. Experimental parameter.

DC-link voltage	$V_{DC}$	350 V
Power grid voltage	$V_{Grid}$	$200 V_{rms}$
Output current	I <sub>out</sub>	$25 \text{ A}_{\text{rms}}$
Switching frequency	$f_{SW}$	10 kHz
Ripple current maximum phase	$\theta_{\textit{ripple_max}}$	38 deg.
Required constant inductance	L const	310 µH
Allowable ripple current ratio	$r_I$	0.4



Fig. 12. Inductor current waveform with the inductor that allowed

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